

1 **How Fractal Complexity Distorts Distance and Elevation Gain in Trail and Mountain**
2 **Running: The Case for Course Measurement Standardisation**

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32 GPS accuracy

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1 **Abstract**

2 Research Question:

3 Trail and mountain running (TMR) is a rapidly growing and increasingly professionalized
4 sport. However, the absence of a common standard for measuring race courses creates
5 inconsistencies in distance and elevation gain metrics. This study investigates how
6 fractal complexity affects these measurements at varying GPS resolutions and
7 emphasizes the need for standardized course measurement protocols in TMR.

8 Research Methods:

9 GPX files from 34 UTMB World Series race courses, including final events in Chamonix,
10 were analysed. Horizontal distance, elevation gain, km-effort, and fractal complexity
11 were computed at varying GPS spatial resolutions (0.2–100 m). Elevation data were
12 refined using a 20-cm Digital Elevation Model (DEM) to minimize errors. Courses were
13 systematically resampled and compared to assess the effects of spatial resolution on
14 race measurements and classifications.

15 Results and Findings:

16 The findings reveal that a decrease a in the spatial resolution of GPS measurements
17 leads to significant reductions in measured horizontal and vertical distances, with
18 discrepancies of up to 10%. These inconsistencies affect race course classifications,
19 athlete benchmarking, and performance comparisons across different events.

20 Implications:

21 This study highlights the importance of standardising GPS spatial resolution to improve
22 the accuracy and consistency of trail and mountain running race measurements.
23 Adopting a 1-metre resolution would enhance the reliability of distance, elevation gain,
24 and km-effort calculations, ensuring fairer race classifications and comparability
25 across events. The proposed methodology can also benefit other sports and disciplines
26 that rely on precise course measurements, such as cycling, hiking, and skiing, by
27 reducing discrepancies caused by varying measurement protocols.

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1 1. Introduction

2 The rising popularity of Trail and Mountain Running (TMR), along with other running
3 disciplines in natural terrain—such as sky, fell, ultra, or cross-country running—has
4 inspired thousands to connect with natural environments, fostering efforts to further
5 develop and organise the sport.

6 TMR courses, often set in diverse and rugged topographies, vary widely in distance,
7 cumulative elevation gain, technical difficulty, and complexity. This variability
8 introduces a unique challenge: the irregular and self-similar (fractal) structure of
9 mountain geography impacts the accuracy of distance measurements, both
10 horizontally and vertically (Skinner, 2020).

11 The fractal nature of geographic features is well-documented in scientific literature
12 (Mandelbrot 1998, Lam & Quattrochi 1992). A renowned study by Mandelbrot (1967)
13 demonstrated how attempts to measure the coastline of Great Britain yielded varying
14 distances depending on the spatial resolution of the measurement. This concept
15 applies to TMR courses, where intricate and repeating patterns in the terrain make
16 distance and elevation measurements highly sensitive to the spatial resolution of
17 course data, typically obtained from global positioning system (GPS) devices (Li, 2014)
18 or Geographical Information Systems (GIS). Even minor changes in resolution can result
19 in substantial differences in reported distances and elevation gains, as reported by
20 Skinner (2020), where the total distance of the Appalachian Trail decreases as the
21 spatial resolution increases.

22 Two consecutive points on a TMR course, recorded with a spatial resolution of 10
23 metres, imply that the athlete's trajectory between them is a straight line. However, the
24 irregularity of natural terrain often makes this assumption inaccurate. If the segment
25 were measured at a finer, human-scale resolution (e.g., 1 metre), the recorded distance
26 would increase, capturing the fractal complexity of the terrain.

27 In road running, established standards for measuring distance and altitude ensure
28 consistency and comparability across events (World Athletics & AIMS, 2023; Corbitt et
29 al., 1964). Tools like the Jones Counter, which measures distances by rolling a
30 standardized wheel along the course, account for both horizontal and vertical
31 displacement, providing accurate three-dimensional measurements for official races.
32 While these mature and widely adopted methods ensure precision in road running, they
33 cannot be used effectively in natural environments with irregular and uneven terrain.

34 In contrast, GPS devices commonly used in TMR, calculate distance based on a two-
35 dimensional model, treating the vertical components of rugged terrain as a separate
36 measure, referred to as elevation gain. This distinction can lead to discrepancies
37 between official distances recorded for road races and those measured by
38 commercially available GPS devices, particularly on hilly courses.

39 Research indicates that GPS devices tend to overestimate road distances by 0.04% to
40 0.28% (Vallan & Realpe, 2022). While this level of accuracy aligns with the minimum
41 uncertainty requirements set by World Athletics, GPS is recommended only for
42 validation purposes in road race measurements rather than as a primary tool (World
43 Athletics & AIMS, 2023). In natural terrain, the importance of GPS resolution becomes

1 more pronounced for accurately measuring distances (Li, 2014) and elevation gain
2 (Campbell et al., 2019). Campbell et al. (2022) observe that high-frequency GPS points
3 may introduce noise, while low-frequency points fail to capture terrain-travel rate
4 relationships. Rampinini et al. (2015) further highlight the impact of sampling frequency
5 on GPS accuracy, noting that only devices with a 10 Hz frequency provide sufficient
6 precision for quantifying distances in team sports, particularly as accuracy diminishes
7 with increased speed. Similarly, Gløersen et al. (2018) demonstrate that speed
8 influences positional deviations in ski data, with higher sampling frequencies improving
9 accuracy.

10 To enhance data quality and accuracy, some studies have implemented latitude-
11 longitude corrections to improve distance estimation in pedestrian locomotion
12 (Campbell et al., 2022). Others have explored the use of Digital Elevation Models (DEM)
13 for obtaining and imputing elevation data (de Smet et al, 2018; Sánchez & Villena, 2020;
14 Sánchez et al., 2024). However, in TMR there is currently no consensus on best
15 practices for measuring either distance or elevation gain.

16 Derived from Naismith’s Rule (Scarf, 2007), the kilometre-effort formula—widely
17 adopted by the International Trail Running Association (ITRA)—adds 1 kilometre of effort
18 (km-effort) for every 100 metres of elevation gain to approximate the physical demands
19 of a course. Using this metric, ITRA classifies races into standardised categories, such
20 as S for Short (45–74 km-effort), M for Medium (75–114 km-effort), L for Long (115–154
21 km-effort), XL for Extra Long (155–209 km-effort), and XXL for Ultra Long (210 km-effort
22 or more). To refine these estimations, more advanced hiking formulas have been
23 proposed, incorporating factors like elevation loss, a nonlinear relationship between
24 slope and speed, or the impact of altitude on route difficulty (Prisner & Sui, 2023; Kay,
25 2012; Emig & Peltonen, 2020; de Smet et al., 2018). Nevertheless, these methods rely
26 heavily on the consistent and accurate measurement of both distance and elevation
27 gain.

28 This paper addresses a critical gap in the literature regarding the standardization of
29 spatial resolution for TMR course measurement. The absence of consistent standards
30 complicates event comparison and course classification, limiting the sport’s formal
31 development. A standardized framework would enable fair comparisons and provide
32 sports scientists with reliable tools to study athletes in real-world environments,
33 enhancing our understanding of athlete’s performance.

34 Given this context, the aim of this paper is to assess how spatial resolution influences
35 the measurement and classification of trail and mountain running courses, with a focus
36 on its implications for distance, elevation gain, and race categorisation.

37 The specific objectives are:

- 38 1. To characterise the current variation in spatial resolution, distance, and elevation
39 gain across UTMB World Circuit, one of the major global TMR event series.
- 40 2. To examine how race distances, elevation gains, and kilometre-effort values
41 change across a wide range of spatial resolutions, comparing these to values
42 derived using a human-scale 1-metre spatial resolution standard.
- 43 3. To assess the impact of adopting a 1-metre spatial resolution standard on race
44 classification systems, particularly concerning ITRA’s race categories.

1 **2. Methods**

2 **2.1. Assessing variation in spatial resolution across the UTMB circuit**

3 The dataset consists of GPX files published online by races within the Ultra-Trail du
4 Mont-Blanc (UTMB) World circuit (UTMB, 2024), which is the most established trail and
5 mountain running series worldwide. For each race event, the longest available distance
6 was selected, resulting in a total of 34 GPX files from different UTMB circuit races
7 available as of November 2024. All distances from the final event, which start and/or
8 finish in Chamonix, France (TDS, CCC, UTMB, OCC, MCC) were also included.

9 For each GPX file, the distance between two consecutive points was calculated using
10 the cosine-haversine formula (Robusto, 1957), which provides the horizontal distance
11 without accounting for vertical displacement. For simplicity, we will refer to horizontal
12 displacement as distance. Vertical displacement between consecutive points was
13 calculated separately, which can result in elevation gain or elevation loss.

14 For the entire course, total distance, cumulative elevation gain, and cumulative
15 elevation loss were computed. The spatial resolution of each course was defined as the
16 average horizontal distance between consecutive points. The kilometre-effort of the
17 course was calculated using the cumulative elevation gain and total distance, based on
18 Naismith's formula (Scarf, 2007).

19 The percentage of measurements with no horizontal displacement between
20 consecutive points was determined (% of idle time) as a measure of data quality.
21 Additionally, elevation gain and loss during idle time were analysed, revealing instances
22 of spurious elevation gain attributed to measurement errors and sensor recalibration.

23 The fractal complexity of each course was calculated using the periodogram estimator
24 (Chan, 1995), offering a measure of the course's geometric complexity.

25 Finally, a descriptive statistical analysis was conducted, reporting global means,
26 standard deviations, quartiles, and median values for all described variables.

27 **2.2. Comparing kilometre-effort, distance and elevation gain across spatial** 28 **resolutions**

29 To compare courses at different spatial resolutions, we first resampled all GPX files to
30 the highest resolution of 0.2 metres using linear interpolation. This method was chosen
31 to avoid potential bias introduced by model-based interpolation techniques. Once all
32 courses were resampled to a 0.2-meter resolution, they were systematically down
33 sampled to resolutions ranging from 0.2 to 100 metres, resulting in 500 versions of each
34 course across the resolution spectrum.

35 To minimize inconsistencies in elevation data, elevation values for each course at each
36 resolution were derived from a Digital Elevation Model (DEM), following the
37 methodology outlined in previous studies (Sanchez & Villena, 2020, Menaspà et al.,
38 2014). The DEM used in this study was sourced from the Shuttle Radar Topography
39 Mission (SRTM) (NASA, 2013), which is globally available and offered at multiple spatial
40 resolutions. To obtain a 20-cm resolution DEM, bilinear interpolation was applied to
41 downscale the SRTM data, as this resolution has been shown to reduce elevation gain
42 measurement errors (Sánchez et al., 2024).

1 For each course and resolution, we then computed horizontal distance, elevation gain,
2 elevation loss, km-effort, and fractal complexity using the criteria explained in the
3 previous section.

4 To explore the impact of course resolution on km-effort, distance, and elevation gain,
5 we performed a graphical analysis. This analysis contrasts, for each course, the
6 relationship between course spatial resolution and km-effort, distance, and elevation
7 gain, each measure presented in separate subplots. Rather than displaying total km-
8 effort (or distance or elevation gain), the graphical analysis shows the relative measure
9 compared to the 1-metre standard. At each resolution, the relative measure then
10 reflects the proportion of the 1-metre standard captured at that resolution. To make the
11 results more accessible, only the five races from the final UTMB event, which start
12 and/or finish in Chamonix, France, will be highlighted in the charts for improved
13 readability and clarity.

14 **2.3. Evaluating the impact of 1-metre spatial resolution on ITRA's race** 15 **categorisation system**

16 To evaluate the effect of 1-metre spatial resolution on ITRA's race categorisation system,
17 each course's km-effort scores and classification—calculated using both raw course
18 data and the 1-metre standard—were compared through graphical analysis.

1 **3. Results**

2 **3.1. Variation in spatial resolution across the UTMB circuit**

3 Table 1 presents descriptive statistics for the 34 UTMB circuit courses included in this
4 study, providing the mean, standard deviation, minimum, first quartile (q1), median
5 (q2), third quartile (q3), and maximum values for the following variables: distance,
6 elevation gain, elevation loss, km-effort, course resolution, fractal complexity, idle time,
7 elevation gain during idle time, and elevation loss during idle time.

8 The average course resolution is 14.9 m, with the variability across events ranging from
9 1.9 m to 39.7 m. As a result, the fractal complexity, which measures geometric
10 complexity, has a mean value of 1.18, with a range between 0.68 and 1.38. Most races
11 exceed 100 km in distance, with an average race distance of 129 km. Elevation gain and
12 loss are approximately symmetric, with average values around 6900 m, as indicated by
13 the similar distributions across all quantiles.

14 In terms of data quality and course measuring protocols, 25% of the courses show that
15 the average time spent stationary (idle time)—when the person measuring the track was
16 not moving—exceeds 2.5%, with one extreme case reaching 24%. During these idle
17 periods, elevation gain is typically minimal, with the third quartile (Q3) value being just 1
18 meter. However, an extreme case recorded 688 metres of elevation gain during GPS
19 inactivity, likely due to measurement pauses and sensor recalibration, underscoring the
20 potential for inaccuracies in such conditions.

21

22 **3.2. Differences in kilometre-effort, distance, and elevation gain across spatial 23 resolutions**

24 Figure 1 shows the first 5 km of the UTMB 170-km course in Chamonix, France, the main
25 event of the circuit. In this example, the horizontal frequency of GPS measurements
26 was resampled to various resolution values, using the minimum, first quartile (q1),
27 median (q2), third quartile (q3), and maximum values observed in the previous section,
28 rounded to the nearest meter, as well as a 1-metre standard. As a result, the measured
29 distance decreased from 4998 m, when using the 1-metre standard, to 4867 m,
30 representing a shortening of the measured running distance by 2.62%. Additionally, as
31 resolution decreased, both the distance and the number of vertices decreased, and the
32 fractal complexity, which reflects the geometrical complexity of the course, was also
33 reduced. This pattern aligns with the changes in resolution observed in the descriptive
34 statistics.

35 Figure 2 displays three panels showing the relationship between horizontal resolution and
36 km-effort, distance, and elevation gain for course resolutions ranging from 0.2 m to
37 100 m, calculated for all 34 courses on the UTMB World circuit. Down-sampling these
38 courses leads to significant reductions in km-effort, distance, and elevation gain across
39 all races. The most notable loss occurs in elevation gain, with certain courses losing up
40 to 30% compared to a standard model with 1-metre resolution. Generally, the reduction
41 in elevation gain ranges from 5% to 20% across most races. Reductions in measured
42 horizontal distance are less dramatic than those in elevation gain but still significant.
43 Races like TDS and UTMB show reductions of 3-4%, while other courses can lose up to

1 6.5% of their length. Most of the courses presented here experience a reduction in km-
2 effort of more than 5% when compared to the standard 1-metre measurement. When
3 the resolution is below 1 meter km-effort, distance and elevation gain continue to
4 increase, but the growth rate is much slower than above 1 meter.

5 **3.3. Impact of 1-metre spatial resolution on ITRA's race categorisation System**

6 Figure 3 compares race classification and km-effort across all races using two
7 protocols: raw original data and data processed at a 1-metre resolution. The results
8 demonstrate the impact of resolution standardisation on race categorisation. While
9 most races remain in their original categories, some shift to a different category when
10 recalculated at the 1-metre standard, emphasizing the significance of standardisation.
11 None of the five UTMB final event races—highlighted in this figure and the previous
12 one—change categories, though subtle variations in their km-effort are evident. Races
13 measured at higher resolutions typically show minimal changes in km-effort, indicated
14 by horizontal lines between the protocols.

15

1 4. Discussion

2 The findings of this study reveal the profound impact of spatial resolution on the
3 accuracy of races on natural terrain, such as trail and mountain running course
4 measurements, carrying significant implications for the sport's ranking systems, race
5 classification systems, performance comparisons, and overall development. By
6 addressing the influence of resolution on key metrics such as distance, elevation gain,
7 and kilometre-effort (km-effort), this study provides a critical foundation for
8 standardizing measurement practices in events held on natural terrain courses.

9 The variability inherent in natural terrains, characterized by fractal complexity,
10 exacerbates the challenges of accurate measurement. Coarse GPS resolutions, such as
11 the average 14.9 metres observed in this study, fail to capture the human-scale details
12 of rugged terrains, leading to significant underestimations of both distance and
13 elevation gain. These inaccuracies, in turn, distort km-effort values, which are crucial
14 for race classification and athlete benchmarking. For example, races measured at
15 coarser resolutions experienced reductions in km-effort exceeding 5%, with some
16 courses losing up to 30% of their elevation gain. Such discrepancies highlight the
17 limitations of current measurement practices and the urgent need for a standardized
18 approach.

19 The adoption of a 1-metre spatial resolution as a standard emerges as a solution (Li
20 2014). This resolution aligns with the level of detail required to accurately represent
21 natural terrain courses at a human-scale, mitigating the distortions introduced by the
22 fractal nature of the terrain. Resampling data to this resolution not only enhances the
23 precision of key metrics but also provides consistency across events, allowing for
24 meaningful comparisons between races and athlete performances. For instance,
25 recalculating km-effort at a 1-metre resolution revealed shifts in race rankings and
26 classifications, emphasizing how inconsistencies in measurement practices can affect
27 the perceived difficulty of events and the integrity of competitive benchmarks.

28 Unexpected findings, such as elevation gain discrepancies during idle time, further
29 illuminate the inconsistencies in current GPX data recording protocols. These variations
30 show the need for standardized criteria in GPX files to ensure data cleanliness and
31 reliability. Additionally, while some courses exhibited minimal changes when
32 recalculated at a 1-metre resolution, others showed substantial shifts, pointing to the
33 influence of both terrain complexity and device accuracy on measurement outcomes.

34 Despite its contributions, this study is not without limitations. The reliance on publicly
35 available GPX files introduces variability in data quality, and while rigorous interpolation
36 methods were applied to enhance resolution, these cannot fully replicate the precision
37 of real-time high-resolution measurements. Additionally, the focus on UTMB races,
38 while providing valuable insights into one of trail and mountain running's most
39 prominent circuits, may limit the generalizability of findings to other contexts. Future
40 research should expand to include a broader range of events and terrain types, as well
41 as field-based validations of GPS and elevation measurement methodologies.

42 The implications of this study are far-reaching. For elite runners, where performances
43 are often separated by narrow margins, the measurement errors associated with
44 inconsistent resolutions could influence rankings and performance indices such as the

1 ITRA index. For instance, the performances of the 1st and the 5th runner at UTMB 2024
2 lie less than 5% apart in terms of time (UTMB, 2024). If km-effort translates linearly into
3 time spent running, this means that, when comparing efforts performed on two courses
4 with theoretically equal distances, but different GPS measurement intervals, the
5 difference in performance of the 1st and the 5th runner at UTMB could potentially lie
6 within the margin of error occurring due to different measurement standards for two
7 different events with equal distances. This standardization may not be relevant for two
8 runners performing in the same race, but it becomes significant when comparing
9 performance indices such as the ITRA index across different races, varied landscapes,
10 and even different editions of the same race—especially as trail and mountain running
11 events often feature minor course modifications every year.

12 The implications of this study extend beyond trail and mountain running. The
13 standardization of distance and elevation gain measurements is equally applicable to
14 other locomotion sports, such as cycling, hiking, skiing, and rowing, among others.
15 These disciplines encounter similar challenges related to GPS variability, barometric
16 recalibration, and the lack of standardized measurement protocols. Implementing
17 approaches like those proposed in this study could significantly improve measurement
18 accuracy and ensure comparability across events in a wide range of sports.

19 **Conclusion**

20 The adoption of a 1-metre resolution standard for measuring the distance and elevation
21 gain of TMR courses would enhance the reliability and accuracy of natural terrain
22 running sports, enabling consistent race classification, and facilitating scientific
23 research on athlete performance in natural environments. Such advancements are
24 essential for the development of sports such as trail and mountain running as a globally
25 recognized discipline with robust benchmarks and reliable metrics.

26

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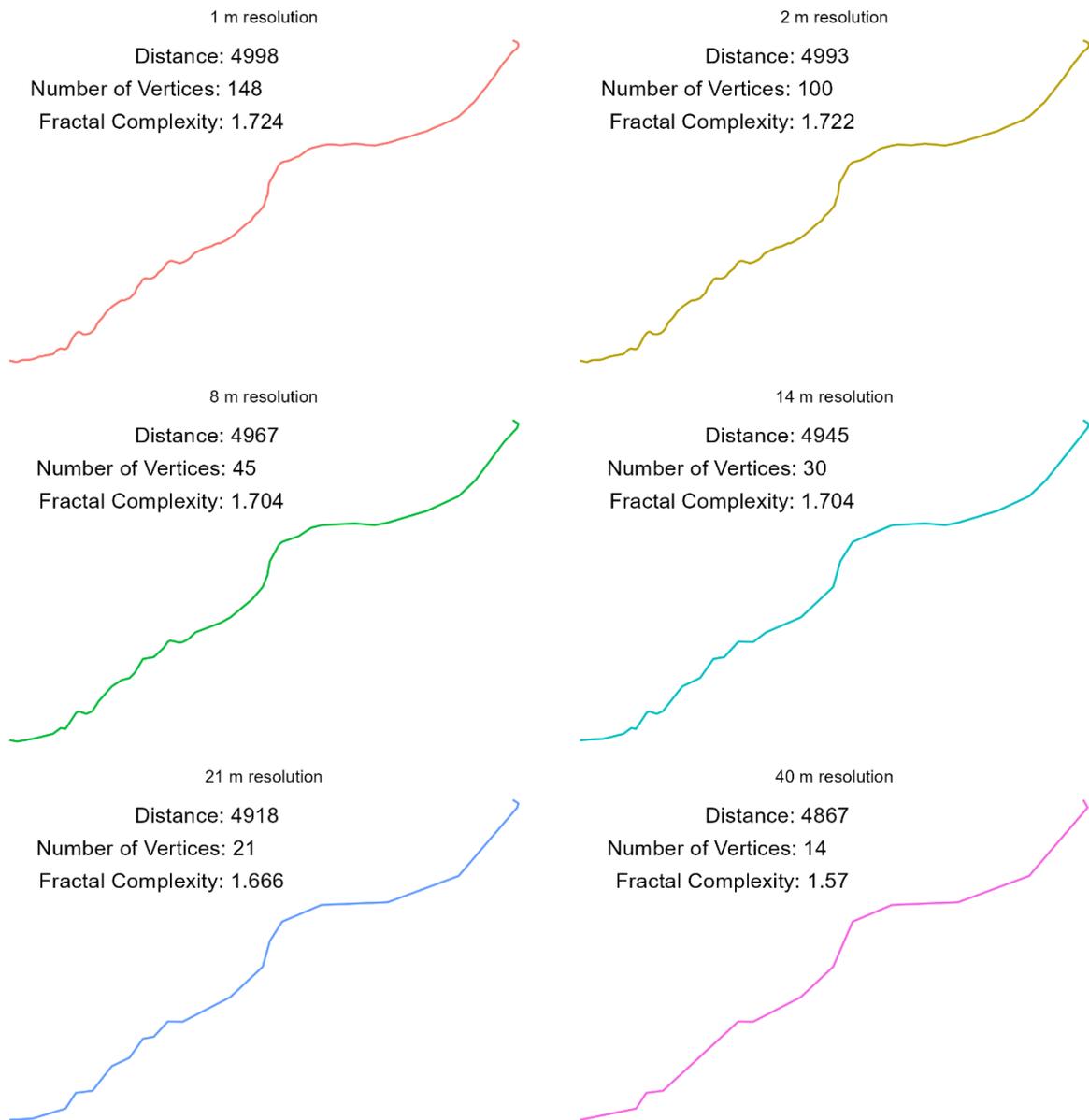
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1 Table 1: Descriptive statistics for all 34 GPX files, including mean, standard deviation
 2 (\pm), [minimum, first quartile (q1), median (q2), third quartile (q3), maximum] values for
 3 distance, elevation gain, elevation loss, km-effort, course resolution, fractal complexity,
 4 idle time, elevation gain during idle time, and elevation loss during idle time.

Variable	Descriptive Statistics
Distance (kms)	129 \pm 45 [38, 100, 123, 161, 258]
Elevation gain (m)	6879 \pm 2883 [2436, 5058, 6312, 8692, 15652]
Elevation loss (m)	6981 \pm 2972 [1894, 5041, 6667, 9236, 15655]
Km-effort	198 \pm 69 [62, 158, 184, 237, 414]
GPS resolution (m)	14.9 \pm 9.4 [1.9, 8.2, 14.2, 21.1, 39.7]
Fractal complexity	1.18 \pm 0.13 [0.68, 1.15, 1.19, 1.24, 1.38]
Idle time (%)	2.3 \pm 4.91 [0, 0.02, 0.16, 2.49, 24.85]
Elevation gain during idle time (m)	32 \pm 122 [0, 0, 0, 1, 688]
Elevation loss during idle time (m)	-5 \pm 13 [-66, -1, 0, 0, 0]

5

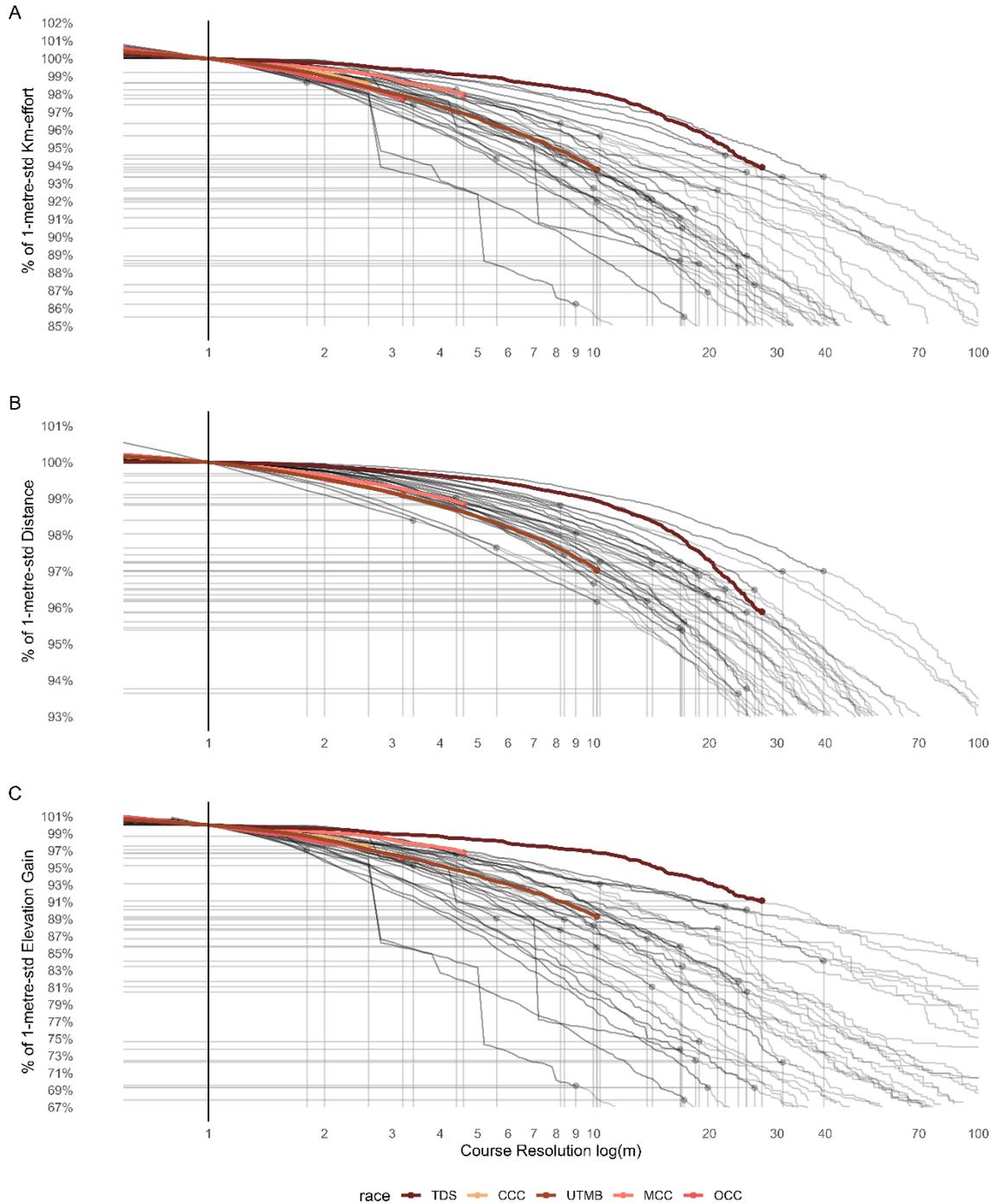
1 Figures:



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3 Figure 1: Stylized map displaying the first 5 km of the UTMB final event in Chamonix,
4 France, at different GPS measurement resolutions.

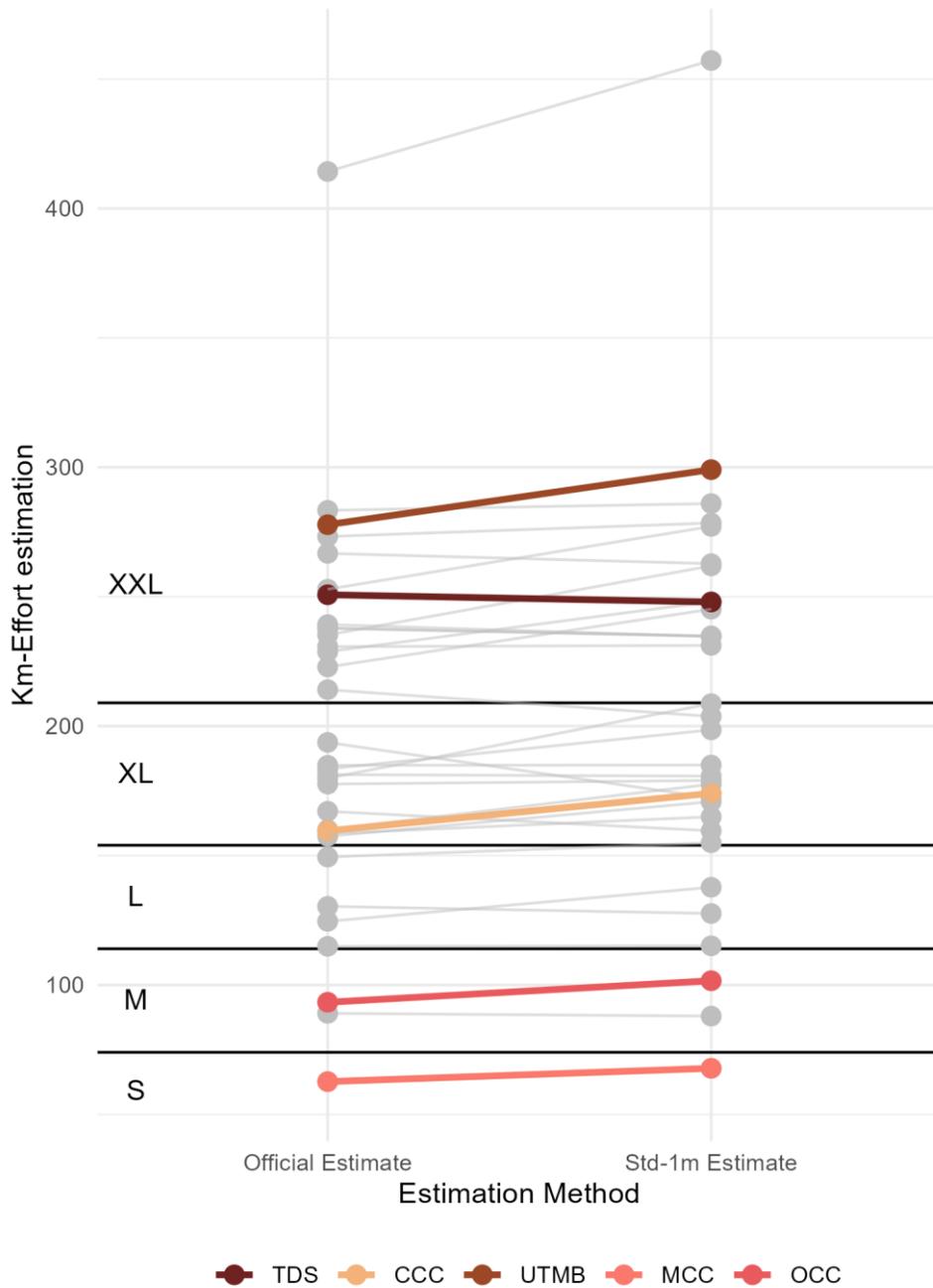
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2 Figure 2: Relationship between course resolution and (A) km-effort, (B) distance, and (C)
 3 elevation gain, shown as percentages relative to the 1-metre standard. The plots
 4 illustrate how total km-effort, distance, and elevation gain decrease as resolution
 5 becomes coarser. A vertical black line at 1-metre resolution marks the reference point
 6 where all curves intersect the 100% value on the vertical axis. Races from the main
 7 UTMB event are labelled and highlighted in colour, while other UTMB World Series races
 8 are represented by grey lines.

9



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2 Figure 3: Comparison of km-effort scores between the original course data and
 3 standardized 1-metre resolution data, highlighting shifts in race classifications. The
 4 horizontal lines represent the thresholds for category changes, based on km-effort.
 5 Races of the main UTMB event are labelled and highlighted in colour, while other races
 6 in the UTMB World Series are depicted as grey lines.